

調和地重力による定常応答.

$$m\ddot{x} + c\dot{x} + kx = -m\ddot{y}_0$$

$$y_0 = a_0 \cos p t \quad a_0 \in \mathbb{R}$$

$$y = \underbrace{y_p}_{\text{特解}} + \underbrace{Y}_{\text{全関数}}$$

$$\ddot{x} + 2h\omega \dot{x} + \omega^2 x = -\ddot{y}_0$$

$$= (-a_0 p^2 \sin p t)'$$

$$= a_0 p^2 \cos p t$$

調和対力の $a_0 p^2$.

$F \cos p t$

定常
応答

特解.

$$y_p = \frac{1}{D^2 + 2h\omega D + \omega^2} a_0 p^2 \cos p t.$$

$$= \frac{a_0 p^2}{\sqrt{(\omega^2 - p^2)^2 + (2h\omega p)^2}} \cos(p t - \theta)$$

$$\theta = \tan^{-1} \left(\frac{2h\omega p}{\omega^2 - p^2} \right)$$